

# Lecture Notes. Cryptography.

Assumptions:

1. Zero-information assumption
2. Public modulus ( $\mathbb{Z}_n$  is known)
3. Public algorithm

Message:

1 | 9 | 0

$K=2$ .  
 $K$  is the key.

+K  
in  $\mathbb{Z}_{10}$

Scrambling  
algorithm

3 | 1 | 2

-K  
in  $\mathbb{Z}_{10}$

Attacker's knowledge:

Everything but  $K$ .  
The system is "secure" because  
attacker must try at most  
ALL VALUES POSSIBLE FOR  $K$ .  
(BRUTE FORCE ATTACK).

Linear cipher. take message  $i$  send to  $ja \times i + b$  in  $\mathbb{Z}_n$ .  
 $a$  must be invertible i.e.  $a \in (\mathbb{Z}_n)^*$ .

Two decryption is  $(j-b) \times a^{-1}$ .

In public-knowledge, want to increase security by  
maximizing largest possible key-search brute force  
algorithm length.

Size of BFKS is at worst  $n \times \phi(n)$ . (Why?)  
for  $b$   $\uparrow$   $\uparrow$  for  $a$ .

Maximize  $n \times \phi(n) \Rightarrow n \times (n-1)$  (when  $n$  prime)

Work on block-sizes for scrambler (permutation).

Vary linear parameters by blocks.

Permutation BFKS worst case? Block size  $k \Rightarrow k!$

Perm/Lin on  $k$  blocks,  $s$  lin, & Perm  $\Rightarrow |BFKS| = s \times k! \times n \times \phi(n)$   
(with known block size!).