

Assignment #4

Yufeng Chinese School Math Enrichment

Name: _____

1. (3) Find $\gcd(64, 24)$ by prime factorization.

$$64 = 2^6$$

$$24 = 2^3 \times 3$$

2. (3) Find $\gcd(64, 24)$ by the Euclidean Algorithm.

$$64 = 24 \times 2 + 16$$

$$24 = 16 \times 1 + 8$$

$$16 = 8 \times 2 + 0$$

$$\gcd(64, 24) = 2^3 = 8$$

3. (4) Using the Extended Euclidean Algorithm, find numbers A and B so that:

$$64xA + 24xB = \gcd(64, 24)$$

| q | 64 | 24 | r |
|---|----|----|----|
| * | 1 | 0 | 64 |
| * | 0 | 1 | 24 |
| 2 | 1 | -2 | 16 |
| 1 | -1 | 3 | 8 |
| 1 | -1 | 3 | 8 |
| 2 | 3 | -8 | 0 |

$$\text{Therefore } 64 \times (-1) + 24 \times (-8) = 8 = \gcd(64, 24)$$