## Problem solving simultaneous equations

## Question 1



A solid cuboid has a volume of $40 \mathrm{~cm}^{3}$.
The cuboid has a total surface area of $100 \mathrm{~cm}^{2}$.
One edge of the cuboid has length 2 cm .
Find the length of a diagonal of the cuboid.
Give your answer correct to 3 significant figures.

## Question 2

Prove algebraically that the straight line with equation $x-2 y=10$ is a tangent to the circle with equation $x^{2}+y^{2}=20$

Input note: write down the coordinates where the tangent touches the circle.
$\qquad$

## Question 3

A cinema sells adult tickets and child tickets.

The total cost of 3 adult tickets and 1 child ticket is $£ 30$.
The total cost of 1 adult ticket and 3 child tickets is $£ 22$.

Work out the cost of an adult ticket and the cost of a child ticket.
adult ticket $£$ $\qquad$
child ticket $£$ $\qquad$

## Question 4

The graph of $x^{2}+y^{2}=12.25$ is drawn below.


Hence find estimates for the solutions of the simultaneous equations

$$
\begin{gathered}
x^{2}+y^{2}=12.25 \\
2 x+y=1
\end{gathered}
$$

## Question 5

Kate buys 2 lollies and 5 choc ices for $£ 6.50$
Pete buys 2 lollies and 3 choc ices for $£ 4.30$
Work out the cost of one lolly.
Give your answer in pence.
$\qquad$ $p$

## Question 6

Here are the first six terms of a Fibonacci sequence.
$\begin{array}{llllll}1 & 1 & 2 & 3 & 5 & 8\end{array}$

The rule to continue a Fibonacci sequence is,
the next term in the sequence is the sum of the two previous terms

The first three terms of a different Fibonacci sequence are
$a \quad b \quad a+b$
We can show that the 6th term of the sequence is $3 a+5 b$
Given that the 3 rd term is 7 and the 6th term is 29 , find the value of $a$ and the value of $b$.

